

# NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY 

FACULTY OF APPLIED SCIENCE

DEPARTMENT OF APPLIED CHEMISTRY

MECHANICAL ENGINEERING

SCH 2205
Supplementary Examination Paper

August 2015

This examination paper consists of 7 pages

Time Allowed: 3 hours
Total Marks: 100
Special Requirements: Calculator, Trigonometry tables (attached)
Examiner's Name: Mr Golden G Nyambuya

## INSTRUCTIONS TO CANDIDATES

Answer ANY FIVE questions. Each question carries 20 marks.
Make use of clear sketches where necessary.

MARK ALLOCATION

| QUESTION | MARKS |
| :--- | :--- |
| 1. | 20 |
| 2. | 20 |
| 3. | 20 |
| 4. | 20 |
| 5. | 20 |
| 6. | 20 |
| TOTAL POSSIBLE MARKS | 100 |

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## Question One (1)

a) Find the resultant of the displacement vectors $\mathrm{A}, \mathrm{B}, \mathrm{C}$, in the $\mathrm{x}-\mathrm{y}$ plane, as shown in the figure below. All the lengths are in metres. [2+2+2 marks]

b) Suppose that a ball is thrown vertically upward with an initial velocity of $30 \mathrm{~m} / \mathrm{s}$. Determine:
(i) How high it will go,
(ii) What velocity it will have as it moves down past its original point of projection,
(iii) Its position 6 sec after it was thrown upwards, and
(iv) The velocity with which it will be moving at this time. [2+2+2+2 marks]
c) The angular velocity of an airplane propeller is increased from 1800 rpm to 2200 rpm in 5 sec . Determine:
(i) Its angular acceleration (in rad $/ \mathrm{s}^{2}$ )
(ii) The angle traversed this period (in radians)

## Question Two (2)

a) A force of 900 N is applied to a mass of 150 kg . Determine:
(i) The acceleration produced
(ii) If the body starts from rest, determine the distance the body travels if the force acts on it for 10 sec .
b) A weight of 100 kg rests on a plank which is inclined at an angle of $30^{\circ}$ with the horizontal, as shown in the figure below. The coefficient of static friction is 0.8 . Calculate:
(i) The normal force on the body
(ii) The frictional force between the block and the plank [3+3 marks]

c) Suppose that a block is pulled along a level floor by a rope making an angle of $30^{0}$ with the floor. The block moves a distance of 15 m . If the force F is 40 N , and the power of the pulling machine is 52 W , calculate:
(i) The work done by the machine
(ii) The time taken for the block to move the distance
(iii) The acceleration of the block
(iv) The final velocity of the block
(v) The kinetic energy of the block at the 15 m mark

## Question Three (3)

a) Define the following terms:
(i) Moment of inertia
(ii) inelastic collision and inelastic collision
b) A Cadillac with a mass of 2100 kg is traveling at 55 mph when it strikes a Volkswagen of mass 1100 kg initially at rest. After the collision the two cars stick together. What is their velocity after the collision?
c) A 0.03 kg bullet if fired from a gun with a velocity of $600 \mathrm{~m} / \mathrm{sec}$. If the gun weighs 2.5 kg , what is the recoil velocity of the gun?
[3 marks]
d) A student with an arm of length 0.6 m holds a suitcase weighing 25 N in her hand. Calculate the torque exerted on her shoulder by the weight if she holds her arm:
(i) Stretched horizontally away from her body
(ii) Hanging it straight down
(iii) At an angle of $60^{\circ}$ below horizontal
e) A 16 ft seesaw is pivoted in the centre. At what distance from the centre would a 200 lb person sit to balance a 150 lb person on the opposite end? (Sketch and label all the important quantities in this calculation)
[2+2 marks]

## Question Four (4)

a) Define the following terms:
(i) Young's modulus
(ii) Stress and Strain
[2 marks]
b) A 1 mm diameter manganese bronze test specimen was subjected to an axial tensile load, and the following data were obtained.

| Gauge length | 10 mm |
| :--- | :--- |
| Final gauge length | 12.25 mm |
| Load at proportional limit | 18.50 N |
| Elongation at proportional limit | 0.016 mm |
| Maximum load | 55.00 N |
| Load at rupture | 42.00 N |
| Diameter at rupture | 0.845 mm |

Calculate the following the following:
(i) Proportional limit. [2 marks]
(ii) Modulus of elasticity. [2 marks]
(iii) Ultimate strength.
[2 marks]
(iv) Percentage elongation.
(v) Percentage reduction in area. [1 mark]
(vi) Indicated rupture strength.
(vii) True rupture strength.

A solid shaft 6 m long is stressed at 80 MPa when twisted through $5^{\circ}$, using $\mathrm{G}=83 \mathrm{MPa}$.
(i) Compute the shaft diameter. [2 marks]
(ii) What power can be transmitted by the shaft at 25 Hz ? [2 marks]

## Question Five (5)

a) State and explain the following:
(i) Bernoulli principle.
[3 marks]
(ii) Archimedes' principle. [3 marks]
(iii) Continuity equation.
b) Oil at $20^{\circ} \mathrm{C}\left(\rho=880 \mathrm{~kg} / \mathrm{cm}^{3}\right.$ and $\left.\mu=0.800 \mathrm{~kg} / \mathrm{m} . \mathrm{s}\right)$ is flowing steadily through an inlet and outlet are measured to be 740 kPa and 90 kPa , respectively. Determine the flow rate of oil through the pipe assuming the pipe is:
(i) Horizontal
[3 marks]
(ii) Inclined at $55^{\circ}$ upwards.
(iii) Inclined $20^{\circ}$ down wards.
(iv) Verify that the flow through the pipe is laminar.

## Question Six (6)

a) A compound belt and counter shaft drive is shown in the diagram below. The pulley diameters are: A 80 cm, B $35 \mathrm{~cm}, \mathrm{C} 62 \mathrm{~cm}$ and D 32 cm .


The power input to the pulley is 15 kw at a speed of $100 \mathrm{rev} / \mathrm{min}$. If the belt drive is $85 \%$ efficient, calculate:
(i) The output power $(\mathrm{kW})$ at D .
(ii) The speed of rotation of $D$.
(iii) The torque exerted at D.
b) A crate of mass 25 kg is pulled up a rough incline with initial speed of $5.00 \mathrm{~m} / \mathrm{s}$. The pulling force is 250 N parallel to the incline which makes an angle $40^{\circ}$ with the horizontal. The coefficient of kinetic friction is 0.500 and the crate is pulled 15.00 m .
(i) How much work is done by gravitational force on the crate? [2 marks]
(ii) Determine the increase in the internal energy due to friction.
[2 marks]
(iii) How much work is done by the 250 N force on the crate?
[2 marks]
(iv) What is the speed of the crate after being pulled 5.00 m ?
[2 marks]

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## Trigonometry Table

| Radian | Degree | Sine | Cosine | Tangent | Radian | Degree | Sine | Cosine | Tangent |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 0 | 0.000 | 1.000 | 0.000 | 0.803 | 46 | 0.719 | 0.695 | 1.036 |
| 0.017 | 1 | 0.017 | 1.000 | 0.017 | 0.820 | 47 | 0.731 | 0.682 | 1.072 |
| 0.035 | 2 | 0.035 | 0.999 | 0.035 | 0.838 | 48 | 0.743 | 0.669 | 1.111 |
| 0.052 | 3 | 0.052 | 0.999 | 0.052 | 0.855 | 49 | 0.755 | 0.656 | 1.150 |
| 0.070 | 4 | 0.070 | 0.998 | 0.070 | 0.873 | 50 | 0.766 | 0.643 | 1.192 |
| 0.087 | 5 | 0.087 | 0.996 | 0.087 | 0.890 | 51 | 0.777 | 0.629 | 1.235 |
| 0.105 | 6 | 0.105 | 0.995 | 0.105 | 0.908 | 52 | 0.788 | 0.616 | 1.280 |
| 0.122 | 7 | 0.122 | 0.993 | 0.123 | 0.925 | 53 | 0.799 | 0.602 | 1.327 |
| 0.140 | 8 | 0.139 | 0.990 | 0.141 | 0.942 | 54 | 0.809 | 0.588 | 1.376 |
| 0.157 | 9 | 0.156 | 0.988 | 0.158 | 0.960 | 55 | 0.819 | 0.574 | 1.428 |
| 0.175 | 10 | 0.174 | 0.985 | 0.176 | 0.977 | 56 | 0.829 | 0.559 | 1.483 |
| 0.192 | 11 | 0.191 | 0.982 | 0.194 | 0.995 | 57 | 0.839 | 0.545 | 1.540 |
| 0.209 | 12 | 0.208 | 0.978 | 0.213 | 1.012 | 58 | 0.848 | 0.530 | 1.600 |
| 0.227 | 13 | 0.225 | 0.974 | 0.231 | 1.030 | 59 | 0.857 | 0.515 | 1.664 |
| 0.244 | 14 | 0.242 | 0.970 | 0.249 | 1.047 | 60 | 0.866 | 0.500 | 1.732 |
| 0.262 | 15 | 0.259 | 0.966 | 0.268 | 1.065 | 61 | 0.875 | 0.485 | 1.804 |
| 0.279 | 16 | 0.276 | 0.961 | 0.287 | 1.082 | 62 | 0.883 | 0.469 | 1.881 |
| 0.297 | 17 | 0.292 | 0.956 | 0.306 | 1.100 | 63 | 0.891 | 0.454 | 1.963 |
| 0.314 | 18 | 0.309 | 0.951 | 0.325 | 1.117 | 64 | 0.899 | 0.438 | 2.050 |
| 0.332 | 19 | 0.326 | 0.946 | 0.344 | 1.134 | 65 | 0.906 | 0.423 | 2.145 |
| 0.349 | 20 | 0.342 | 0.940 | 0.364 | 1.152 | 66 | 0.914 | 0.407 | 2.246 |
| 0.367 | 21 | 0.358 | 0.934 | 0.384 | 1.169 | 67 | 0.921 | 0.391 | 2.356 |
| 0.384 | 22 | 0.375 | 0.927 | 0.404 | 1.187 | 68 | 0.927 | 0.375 | 2.475 |
| 0.401 | 23 | 0.391 | 0.921 | 0.424 | 1.204 | 69 | 0.934 | 0.358 | 2.605 |
| 0.419 | 24 | 0.407 | 0.914 | 0.445 | 1.222 | 70 | 0.940 | 0.342 | 2.747 |
| 0.436 | 25 | 0.423 | 0.906 | 0.466 | 1.239 | 71 | 0.946 | 0.326 | 2.904 |
| 0.454 | 26 | 0.438 | 0.899 | 0.488 | 1.257 | 72 | 0.951 | 0.309 | 3.078 |
| 0.471 | 27 | 0.454 | 0.891 | 0.510 | 1.274 | 73 | 0.956 | 0.292 | 3.271 |
| 0.489 | 28 | 0.469 | 0.883 | 0.532 | 1.292 | 74 | 0.961 | 0.276 | 3.487 |
| 0.506 | 29 | 0.485 | 0.875 | 0.554 | 1.309 | 75 | 0.966 | 0.259 | 3.732 |
| 0.524 | 30 | 0.500 | 0.866 | 0.577 | 1.326 | 76 | 0.970 | 0.242 | 4.011 |
| 0.541 | 31 | 0.515 | 0.857 | 0.601 | 1.344 | 77 | 0.974 | 0.225 | 4.331 |
| $0.559$ | 32 | $0.530$ | 0.848 | 0.625 | $1.361$ | 78 | 0.978 | 0.208 | 4.705 |
| $0.576$ | 33 | $0.545$ | $0.839$ | 0.649 | $1.379$ | $79$ | $0.982$ | $0.191$ | 5.145 |
| 0.593 | $34$ | $0.559$ | 0.829 | 0.675 | $1.396$ | $80$ | $0.985$ | 0.174 | 5.671 |
| $0.611$ | $35$ | $0.574$ | $0.819$ | 0.700 | $1.414$ | $81$ | $0.988$ | $0.156$ | 6.314 |
| $0.628$ | $36$ | $0.588$ | $0.809$ | $0.727$ | $1.431$ | $82$ | $0.990$ | $0.139$ | 7.115 |
| 0.646 | 37 | $0.602$ | 0.799 | $0.754$ | $1.449$ | $83$ | $0.993$ | $0.122$ | $8.144$ |
| $0.663$ | $38$ | $0.616$ | $0.788$ | $0.781$ | $1.466$ | $84$ | $0.995$ | $0.105$ | $9.514$ |
| $0.681$ | $39$ | $0.629$ | $0.777$ | $0.810$ | $1.484$ | $85$ | $0.996$ | $0.087$ | $11.430$ |
| $0.698$ | 40 | $0.643$ | $0.766$ | $0.839$ | $1.501$ | $86$ | $0.998$ | $0.070$ | $14.301$ |
| $0.716$ | $41$ | $0.656$ | $0.755$ | $0.869$ | $1.518$ | $87$ | $0.999$ | $0.052$ | $19.081$ |
| $0.733$ | $42$ | $0.669$ | $0.743$ | $0.900$ | $1.536$ | $88$ | $0.999$ | $0.035$ | $28.636$ |
| $0.750$ | $43$ | $0.682$ | $0.731$ | $0.933$ | $1.553$ | $89$ | $1.000$ | $0.017$ | $57.290$ |
| $0.768$ | $44$ | $0.695$ | $0.719$ | $0.966$ | $1.571$ | $90$ | $1.000$ | $0.000$ | $\infty$ |
| 0.785 | 45 | 0.707 | 0.707 | 1.000 |  |  |  |  |  |

