

# NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY

## APPLIED PHYSICS DEPARTMENT

### SPH 1106 MODERN PHYSICS FOR CHEMISTS

BSc HONOURS PART I: JANUARY 2004

DURATION : 3 HOURS

ANSWER ALL PARTS OF QUESTION 1 IN SECTION A AND ANY THREE QUESTIONS FROM SECTION B. SECTION A CARRIES 40 MARKS AND SECTION B CARRIES 60 MARKS

Planck's constant,	$h = 6.63 \times 10^{-34} \text{ J.s}$
Electron rest mass,	$m_e = 9.11 \times 10^{-31} \text{ kg}$
Speed of light,	$c = 3.00 \times 10^8 \text{ m s}^{-1}$
1 electron volt	$e = 1.60 \times 10^{-19} \text{ J}$
Mass of electron,	$m_e = 5.48 \times 10^{-4} \text{ u}$
Mass of proton,	$m_p = 1.007 825 \text{ u}$
Mass of neutron,	$m_n = 1.008 665 \text{ u}$
1 atomic mass unit,	$1\text{u} = 931.49 \text{ MeV}/c^2$
Electronic Charge,	$e = 1.60 \times 10^{-19} \text{ C}$
Stefan – Boltzmann constant	$\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$
Wein's constant,	$k = 2.899 \times 10^{-3} \text{ m} \cdot \text{K}$
Mass of ${}^4\text{H}_e$	${}^4\text{H}_e = 4.002 603\text{u}$
Mass of ${}^1\text{H}$	${}^1\text{H} = 1.007825\text{u}$

#### SECTION A

1. (a) For the photoelectrical effect, define the following terms:
- (i) work function,
  - (ii) photoelectron,
  - (iii) threshold frequency,
  - (iv) write down the photoelectric equation [5]
- (b) (i) What is the "ULTRAVIOLET CATASTROPHE"? [2]  
(ii) For a black body at a temperature of 800k, find the wavelength of the most intense part of radiation that it emits. [3]
- (c) (i) State Bohr's postulates as well as the one he adopted from

- Rutherford for his model of the atom. [3]
- (ii) What does the "Ground state" mean for the hydrogen atom and why is energy associated with this state negative? [4]
- (iii) State Wien's displacement law defining all symbols and explain why it is called a "Displacement Law" [3]
- (d) (i) Why does the "Photoelectric effect" not work for free electrons? [2]
- (ii) A source emits light of wavelength  $4.5 \times 10^{-7} \text{m}$  at a rate of 1.1W. How many photons leave the source every second? [4]
- (e) A baseball player dispatches the ball of mass 150g at a speed of 115km/h. Determine its De Broglie wavelength. [2]
- (f) (i) Define the terms "isotopes", "isotones" and "isobars" in terms of the mass number, A, neutron number N, and the atomic number Z. Give an example of each. [4]
- (ii) The most abundant isotope of helium is  ${}^4_2\text{He}$ . Using atomic mass units and electron volts, Determine the mass deficit and the binding energy per nucleon of  ${}^4_2\text{He}$ . [4]
- (g) Differentiate between continuous and line spectra and explain how you would go about producing each. [2]
- (h) Write a statement for Heisenberg's principle of uncertainty and write down the relationship for position and momentum. [2]

### SECTION B

2. (a) (i) What is your understanding of a 'black body'? [4]
- (ii) Show that in the limits of long wavelengths, Planck's radiation equation given by:
- $$R(\lambda) = \frac{2\pi c^2 h}{\lambda^5} \cdot \frac{1}{e^{hc/\lambda kT} - 1}$$
- reduces to Rayleigh -- Jeans equation or relation. [5]
- (iii) Show that for the most intense part of radiation, Planck's radiation relation reduces to Wein's displacement law. [8]

- (iv) Assuming that the earth has a mean temperature of 300K, determine the power radiated from  $1\text{cm}^2$  of the earth. [3]

3. (a) Define the terms “fusion” and “fission”. [2]  
 (b) Define life time  $T$  and half life  $T_{\frac{1}{2}}$  as applied to radioactive decay. [4]  
 (c) (i) The following table shows the results of measuring the dependence of the activity  $A$  of a certain radioactive element on time  $t$ .

$t(\text{hrs})$	0	3	6	9	12	15
$A(\text{mCi})$	21.6	12.6	7.6	4.2	2.4	1.8

Find the half life of this element. [5]

- (ii) A radioactive substance with decay constant  $\lambda$  has an activity  $A_1$  at  $t = t_1$  and activity  $A_2$  at  $t = t_2$ . What is the total number of atoms that have decayed between  $t_1$  and  $t_2$ ? [5]  
 (d) Calculate the disintegration energy  $Q$  for the Beta decay of  $^{32}\text{P}$ , given that the atomic masses are 31.97391U for  $^{32}\text{P}$  and 31.97207U for  $^{32}\text{S}$ . [4]
4. (a) (i) Show that the radius for the  $n^{\text{th}}$  orbit of Bohr’s model of the hydrogen atom is given by:

$$r_n = \left( \frac{4\pi\epsilon_0\hbar^2}{me^2} \right) n^2 \quad [5]$$

- (ii) Show also, that the energy of the electron in the  $n^{\text{th}}$  orbit is given by:

$$E_n = \frac{-me^4}{32\pi^2\epsilon_0^2\hbar^2 n^2} \quad [5]$$

- (iii) Hence or otherwise find an expression for the energy quantum required to excite a hydrogen atom in its ground state to its “third excited state”. [3]  
 (b) (i) List any three deficiencies of Bohr’s model. [3]  
 (ii) What weaknesses led to Thomson’s ‘plum pudding’ model being discarded? [4]

5. (a) (i) Briefly describe Compton's experiment and explain how it can be used as a basis to support the particulate nature of electromagnetic radiation. [4]
- (ii) Show, using diagrammatic illustrations, that the expression for the Compton shift,  $\Delta\lambda$  is given by:  

$$\lambda' - \lambda = \frac{h}{mec}(1 - \cos\theta)$$
 where  $\theta$  is the scattering angle of the photon. [8]
- (b) In a Compton scattering experiment, x-rays of wavelength 0.015nm are scattered through an angle of  $45^\circ$  by 'free' electrons, what is their new wavelength. [2]
- (c) At what angle  $\theta$  does the maximum possible wavelength of the scattered x-rays occur. [2]
- (d) Explain why in the Compton scattering experiment, the recoil electrons are regarded as 'free'. [2]
- (e) What would be the effect of replacing electrons by protons? [2]
6. (a) What features of the photoelectric effect could not be explained by classical physics? How does Einstein explain these features? [6]
- (b) When sodium metal is illuminated with light of wavelength  $3.10 \times 10^2 \text{ nm}$ , the stopping potential is 1.69V.
- (i) Define the term 'stopping potential' [2]
- (ii) Find the 'work function' of sodium. [3]
- (iii) Calculate the kinetic energy of the most energetic electrons emitted from the sodium surface when it is illuminated with light of wavelength  $2.9 \times 10^2 \text{ nm}$ . [2]
- (iv) Why do some electrons have kinetic energies smaller than  $K_{\text{max}}$ ? [2]
- (c) In the photoelectric effect how can a photon moving in one direction eject an electron moving in a different direction? What happens to conservation of momentum? [2]
- (d) Briefly explain the phrase 'wave-particle duality' [3]

- END OF EXAMINATION -