NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY

FACULTY OF APPLIED SCIENCE COMPUTER SCIENCE DEPARTMENT DECEMBER EXAMINATIONS 2004

SUBJECT: SIMULATION AND MODELLING

CODE: SCS 4108

INSTRUCTIONS TO CANDIDATES:

This Examination paper consists of seven questions (7) All questions carry equal marks
Answer any FIVE (5) questions

TIME: 3HOURS

QUESTION ONE

Use the chi-square test with α =0,05 to test whether the data shown below are uniformly distributed. In the test use 10 intervals of equal length, namely [0, 0.1], [0.1, 0.2],..., [0.9, 1.0]. Given that X^2 0.05, 9 =16,9

| 0.34 | 0.90 | 0.25 | 0.89 | 0.87 | 0.44 | 0.12 | 0.21 | 0.46 | 0.67 |
|------|------|------|------|------|------|------|------|------|------|
| 0.83 | 0.76 | 0.79 | 0.64 | 0.70 | 0.81 | 0.94 | 0.74 | 0.22 | 0.74 |
| 0.96 | 0.99 | 0.77 | 0.67 | 0.56 | 0.41 | 0.52 | 0.73 | 0.99 | 0.02 |
| 0.47 | 0.30 | 0.17 | 0.82 | 0.56 | 0.05 | 0.45 | 0.31 | 0.78 | 0.05 |
| 0.79 | 0.71 | 0.23 | 0.19 | 0.82 | 0.93 | 0.65 | 0.37 | 0.39 | 0.42 |
| 0.99 | 0.17 | 0.99 | 0.46 | 0.05 | 0.66 | 0.10 | 0.42 | 0.18 | 0.49 |
| 0.37 | 0.51 | 0.54 | 0.01 | 0.81 | 0.28 | 0.69 | 0.34 | 0.75 | 0.49 |
| 0.72 | 0.43 | 0.56 | 0.97 | 0.30 | 0.94 | 0.96 | 0.58 | 0.73 | 0.05 |
| 0.06 | 0.39 | 0.84 | 0.24 | 0.40 | 0.64 | 0.40 | 0.19 | 0.79 | 0.62 |
| 0.18 | 0.26 | 0.97 | 0.88 | 0.64 | 0.47 | 0.60 | 0.11 | 0.29 | 0.78 |
| | | | | | | | | | |

QUESTION TWO

| a) | Outline the disadvantages of simulation | [3] |
|----|------------------------------------------------------------------------|-----|
| b) | What do you understand by the term <i>system</i> ? | [1] |
| c) | Describe the components of a system. | [5] |
| d) | Distinguish between <i>deterministic</i> and <i>stochastic</i> models. | [4] |
| e) | Briefly discuss one method of random number generation. | [7] |

QUESTION THREE

| a) | Draw a flow diagram to show service-just completed. | [5] |
|----|----------------------------------------------------------|------|
| b) | Briefly describe the characteristics of queuing systems. | [10] |

c) Use the linear congruential method to generate a sequence of three two-digit random integers. Let $X_0 = 27$, a = 8, c = 47, and m = 100. [5]

QUESTION FOUR

- a) The sequence of numbers 0.54, 0.73, 0.98, 0.11 and 0.68 has been generated. Use the Kolmogorov-Smirnov test with α =0.05 to determine if the hypothesis that the numbers are uniformly distributed on the interval [0,1] can be rejected. [10]
- b) Outline the four steps in the development of a useful model of input data.
- c) Briefly explain the following terms:

i. Event [1]
ii. Activity [1]

QUESTION FIVE

- a) Discuss two tests for Random Numbers [4]b) When do we use the terms *endogenous* and *exogenous* in simulation systems?
- [4]
- c) Distinguish between a *static* simulation model and a *dynamic* simulation model.
- d) Briefly discuss any two steps in a simulation study

[6]

QUESTION SIX

A small grocery has only one till. Customers arrive at the till at random from 1 to 10 minutes apart. The service distributions are shown in table 2.1. The random digits are given in table 2.2.

Table 2.1

| Service Time (min) | 1 | 2 | 3 | 4 | 5 | 6 |
|--------------------|------|-----|-----|-----|------|------|
| Probability | 0.05 | 0.1 | 0.2 | 0.3 | 0.25 | 0.10 |

Table 2.2

| Customer | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|---------------------------|----|----|----|----|----|----|----|----|----|----|
| Random Digits for Arrival | - | 26 | 98 | 90 | 26 | 42 | 74 | 80 | 68 | 22 |
| Random Digits for Service | 95 | 21 | 51 | 92 | 89 | 38 | 13 | 61 | 50 | 49 |

- i. Develop the simulation table and analysis for customers.
- [11]

ii. What is the average waiting time for a customer?

[3]

| iii. iv. | What is the utilization of the teller? What is the average time a customer spends in the system? | [3] [3] |
|----------------|--------------------------------------------------------------------------------------------------|------------|
| QUE | STION SEVEN | |
| a) | | [10 |
| b | Discuss the limitations of simulation. | [4] |
| c [°] | Describe three types of simulation modeling methods. | [6] |

END OF QUESTION PAPER

GOOD LUCK!