

NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY
FACULTY OF APPLIED SCIENCE
COMPUTER SCIENCE DEPARTMENT
DECEMBER EXAMINATIONS 2001

SUBJECT: DIGITAL SIGNALS PROCESSING
CODE: SCS 6101

INSTRUCTION TO CANDIDATES

Answer any four (4) questions.
Each question carries 25 marks

Time: 3 hours

QUESTION ONE

- a) What are the classification of Discrete-time systems and distinguish between them. [8]
- b) Test whether the following Discrete-time signals are periodic, if it is periodic find its fundamental period. [5]
- $x(n) = 5 \sin(2n)$
- c) Find whether the system $y(n) = Ax(n) + B$ is
- i) Linear
 - ii) Time invariant
 - iii) Casual
 - iv) Stable [12]

QUESTION TWO

- a) Write the expressions for
- i) An arbitrary discrete time signal $x(n)$ resolved into Impulses. [1]
 - ii) Linear convolution. [1]
 - iii) Graphical representation of the following discrete time signal. [2]
- $x(n) = (-2)^n u(n)$

Convolve the sequences given

$$h(n) = 5(3)^n u(n)$$

$$x(n) = 4(-2)^n u(n) \quad [11]$$

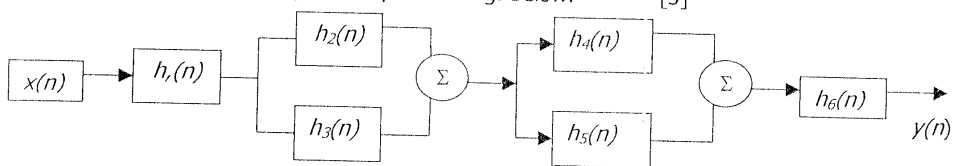
Find the DFT of the sequence

$$x(n) = \{1, 2, 2, 1\} \quad [10]$$

QUESTION THREE

- i) An LTI system has the Impulse response $h(n) = \left(\frac{3}{4}\right)^n u(n)$. Determine the output of the system at times $n = -5$, $n = +5$ and $n = 10$ when input $x(n) = u(n)$ [10]

- ii) Find the expression for impulse response relating to input $x(n)$ or $x(t)$ to the output $y(n)$ or $y(t)$ in terms of the impulse response of each subsystem for the LTI system depicted in fig. Below. [3]



- b) Let $h_1(t)$, $h_2(t)$, $h_3(t)$ and $h_4(t)$ be the impulse responses of LTI system construct a system with impulse response $h(t)$ using $h_1(t)$, $h_2(t)$, $h_3(t)$ and $h_4(t)$ as sub system. Draw the interconnection of systems required to obtain
- $$h(t) = h_1(t) * h_2(t) + h_3(t) * h_4(t) \quad [3]$$
- c) Define the elementary signals $\delta(t)$, $u(t)$ and $r(t)$ and bring out the relation between them. [6]

Define stability of a system.

[3]

QUESTION FOUR

- a) i) What are FIR and IIR systems. Give examples.
ii) Bring out the advantages of FIR filter compared to IIR filters.

[5]

- b) A discrete time system has a unit sample response $h(n)$ given by

$$h(n) = \frac{1}{2}\delta(n) + \delta(n-1) + \frac{1}{2}\delta(n-2)$$

[15]

Find the frequency response $H(e^{j\omega})$. Plot its magnitudes phase.

- c) Find the convolution of the below finite sequence:

$$x(k) = \left\{ \frac{1}{2}, 2, 1, -1 \right\}$$

$$h(k) = \left\{ 2, 1, \frac{1}{2} \right\}$$

[5]

QUESTION FIVE

- a) Briefly explain

- i) aliasing
ii) FFT
iii) Determine the sampling frequency for the following signals

$$x(t) = \sin 200\pi t + \cos 300\pi t + \sin 400\pi t$$

[6]

- b) Find the circular convolution of the following two sequences

$$x(n) = \{0, 1, 2, 3\}$$

↑

$$h(n) = \{2, 1, 1, 2\}$$

↑

[7]

Realize the following transfer function as Direct form I and II structure

$$H(z) = \frac{8z^3 - 4z^2 + 4z - 2}{(z - \frac{1}{4})(z^2 - z + \frac{1}{2})} \quad [12]$$

QUESTION SIX

With the help of block diagrams, explain how DSP techniques can be used for any one application. [25]

END OF QUESTION PAPER

GOOD LUCK!