#### **BACHELOR OF COMMERCE (HONOURS) DEGREE**

#### **QUANTITATIVE ANALYSIS FOR BUSINESS CIN 1106**

#### SUPPLEMENTARY EXAMINATION JULY 2001 **DURATION: 3 HOURS**

#### **INSTRUCTIONS TO CANDIDATES**

- 1. Answer all questions in Section A
- 2. Choose and answer three(3) out of (5) questions in Section B
- 3. Answer both questions in Section C
- Graph paper will be provided
  Statistical tables will be provided
- 6. You may use a non-programmable Scientific Calculator

# **SECTION A (ANSWER ALL QUESTIONS)** [40 MARKS]

#### **QUESTION ONE**

a) A manufacturer of light bulbs finds that the total cost 'C' of producing x units of a product is given by :

$$C(x) = 0,001x^3 - 0,21x^2 + 40x + 1000$$

Determine the marginal cost when the level of production is x=50.

[5 marks]

[5 marks] [5 marks]

b) For the following distribution of marks:

No. of	10	20	15	8	3
Students					
Marks	1-<20	20-<40	40-<60	60-<80	80-<100

Calculate:

- ii) the Median
- c) Maximize:

$$\mathbf{Z}=\mathbf{2}\mathbf{x}_1+\mathbf{3}\mathbf{x}_2$$

Subject to:  $x_1 + x_2 \le 100$ 

$$4x_1 + 8x_2 \le 500$$

$$x_1, x_2 \ge 0$$

[10 marks]

d) Find the solution set for each of the following inequalities:

i) 4x/(x-4) >3 ii) 7x-2 < (4x-2)/3

# [10 marks]

e) A manufacturer produces 2 products, 1 and 2. One unit of product 1 requires 3 parts of type A and 2 parts of type B. One unit of product 2 requires 1 type A part, 4 type B parts and 2 type C parts. Use a 2x3 Matrix to depict the information.

# [5 marks]

## SECTION B (CHOOSE AND ANSWER 3 OUT OF 5 QUESTIONS) [60 MARKS]

The following table relates to a 3 Industry Economy:

PRODUCER	AGRICULTURE      INDUSTRY      TRANSPORT			FINAL CONSUMER
				DEMAND
AGRICULTURE	12	12	5	31
INDUSTRY	8	24	10	38
TRANSPORT	5	16	8	11

If consumer demand for agriculture is predicted to increase to 35, Industry to 40 and transport to 12, what is the required level of output to satisfy the new demand?

# [20 marks]

# **QUESTION THREE**

a) The population of bacteria (in millions) present in a culture at time 't' is given by:

N(t) = (t-8)(5t) + 40.

At what rate is the population changing at time t=3; t=5?

- b) A firm estimates that the number 'N' of units of a product sold after spending x dollars on advertising is given by N(x) = -0.1x2 + 200x + 60.
  - i) How many units are sold when \$ 500,00 is spent on advertising?
  - ii) What is the instantaneous rate of change of the number of units sold with respect to the amount spent on advertising
  - iii) What is the instantaneous rate of change in sales at x=900; x=1000? [20 marks]

# **QUESTION FOUR**

Lucky Luke has decided to set up a Sinking Fund for the purpose of purchasing a HI-FI system. He will need \$ 30 000 in two years time while the fund will earn 10% interest compounded quarterly.

- a) calculate the regular deposit, R.
- b) Construct the Sinking Fund Schedule
- c) What is the Accumulated Fund after the 3<sup>rd</sup> deposit?

## [20 marks]

#### **QUESTION FIVE**

Using the Gauss-Jordan method, find the inverse of the matrix below, if it exists:

φ1	2	3 κ
2	3	4
λ1	2	1μ

b) Use matrix methods to solve the following system of linear equations:

$$2x_1 + 6x_2 - x_3 = 18$$
$$x_2 + 3x_3 = 9$$
$$3x_1 - 5x_2 + 8x_3 = 4$$

[20 marks]

#### **QUESTION SIX**

Given R(x) = 50x

$$C(x) = 2x^3 - 12x^2 + 40x + 10,$$

Find:

a) P(x) b) R(2),C(2), P(2) c)  $R^*(x), C^*(x), P^*(x)$  d)  $R^*(2), C^*(2), P^*(2)$ 

What is your interpretation of the Marginal revenue function  $R^{*}(x)$  in this problem?

f) What is your interpretation of your Marginal cost function in this problem, vis-à-vis fixed cost?

[20 marks]

#### <u>SECTION C (COMPULSORY)</u> [40 MARKS]

You borrow \$ 30 000 from the bank for purposes of paying for your Post-graduate Project. If Interest is charged at the rate of 16% Compounded quarterly and the loan is for a period of 2 years,

a) Calculate the Regular payment, R.

- b) Construct the relevant Amortization schedule.
- c) How much is outstanding after the 6<sup>th</sup> payment?
- d) What are the Interest and Capital portions of the 5<sup>th</sup> payment?

[20 marks]

# **QUESTION EIGHT**

a) What are the problems(points to note) in the construction of Index numbers?

[8 marks]

b) The table below shows the unit price and quantity of rice, sugar and salt consumed by a certain household in 1996 and 1998.

	1996		1998	
PRODUCT	<b>PRICE \$</b>	QUANTITY(KG)	<b>PRICE \$</b>	QUANTITY(KG)
RICE	12	25	18	15
SUGAR	24	30	37	24
SALT	2,7	6	6,5	6

## (1996=100)

Calculate:

- i) The Unweighted Aggregative Price Index.
- ii) Fischer's Ideal Index

[12 marks] [Total: 20 marks]

# END OF EXAMINATION