## BACHELOR OF COMMERCE (HONOURS) DEGREE

## QUANTITATIVE ANALYSIS FOR BUSINESS CIN 1106

## SUPPLEMENTARY EXAMINATION JULY 2001

DURATION: 3 HOURS

## INSTRUCTIONS TO CANDIDATES

1. Answer all questions in Section A
2. Choose and answer three(3) out of (5) questions in Section B
3. Answer both questions in Section C
4. Graph paper will be provided
5. Statistical tables will be provided
6. You may use a non-programmable Scientific Calculator

## SECTION A (ANSWER ALL QUESTIONS)

[40 MARKS]

## QUESTION ONE

a) A manufacturer of light bulbs finds that the total cost ' C ' of producing x units of a product is given by :

$$
C(x)=0,001 x^{3}-0,21 x^{2}+40 x+1000
$$

Determine the marginal cost when the level of production is $\mathrm{x}=50$.
[5 marks]
b) For the following distribution of marks:

| No. of <br> Students | 10 | 20 | 15 | 8 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Marks | $1-<20$ | $20-<40$ | $40-<60$ | $60-<80$ | $80-<100$ |

Calculate:
i) the Mode
[5 marks]
ii) the Median
[5 marks]
c) Maximize:

$$
\mathbf{Z}=2 \mathbf{x}_{1}+3 \mathbf{x}_{2}
$$

Subject to: $\quad x_{1}+x_{2} \leq 100$

$$
4 x_{1}+8 x_{2} \leq 500
$$

$$
\mathrm{x}_{1}, \mathrm{x}_{2} \geq 0
$$

[10 marks]
d) Find the solution set for each of the following inequalities:
i) $4 x /(x-4)>3$
ii) $7 x-2<(4 x-2) / 3$
[10 marks]
e) A manufacturer produces 2 products, 1 and 2 . One unit of product 1 requires 3 parts of type A and 2 parts of type B. One unit of product 2 requires 1 type A part, 4 type B parts and 2 type C parts. Use a $2 x 3$ Matrix to depict the information.

## [5 marks]

## SECTION B (CHOOSE AND ANSWER 3 OUT OF 5 QUESTIONS)

 [60 MARKS]The following table relates to a 3 Industry Economy:
USER

| PRODUCER | AGRICULTURE | INDUSTRY | TRANSPORT | FINAL <br> CONSUMER <br> DEMAND |
| :--- | :--- | :--- | :--- | :--- |
| AGRICULTURE | 12 | 12 | 5 | 31 |
| INDUSTRY | 8 | 24 | 10 | 38 |
| TRANSPORT | 5 | 16 | 8 | 11 |

If consumer demand for agriculture is predicted to increase to 35 , Industry to 40 and transport to 12 , what is the required level of output to satisfy the new demand?

## [20 marks]

## QUESTION THREE

a) The population of bacteria (in millions) present in a culture at time ' t ' is given by:

$$
\mathrm{N}(\mathrm{t})=(\mathrm{t}-8)(5 \mathrm{t})+40 .
$$

At what rate is the population changing at time $t=3 ; \mathrm{t}=5$ ?
b) A firm estimates that the number ' N ' of units of a product sold after spending $x$ dollars on advertising is given by $N(x)=-0,1 x 2+200 x+60$.
i) How many units are sold when $\$ 500,00$ is spent on advertising?
ii) What is the instantaneous rate of change of the number of units sold with respect to the amount spent on advertising
iii) What is the instantaneous rate of change in sales at $x=900$; $\mathrm{x}=1000$ ?
[20 marks]

## QUESTION FOUR

Lucky Luke has decided to set up a Sinking Fund for the purpose of purchasing a HIFI system. He will need \$ 30000 in two years time while the fund will earn $10 \%$ interest compounded quarterly.
a) calculate the regular deposit, R .
b) Construct the Sinking Fund Schedule
c) What is the Accumulated Fund after the $3^{\text {rd }}$ deposit?
[20 marks]

## QUESTION FIVE

Using the Gauss-Jordan method, find the inverse of the matrix below, if it exists:

b) Use matrix methods to solve the following system of linear equations:

$$
\begin{array}{r}
2 x_{1}+6 x_{2}-x_{3}=18 \\
x_{2}+3 x_{3}=9 \\
3 x_{1}-5 x_{2}+8 x_{3}=4
\end{array}
$$

[20 marks]

## QUESTION SIX

Given $R(x)=50 x$

$$
C(x)=2 x^{3}-12 x^{2}+40 x+10
$$

Find:
a) $P(x)$
b) $\mathrm{R}(2), \mathrm{C}(2), \mathrm{P}(2)$
c) $\mathrm{R} *(\mathrm{x}), \mathrm{C} *(\mathrm{x}), \mathrm{P} *(\mathrm{x})$
d) $\mathrm{R} *(2), \mathrm{C} *(2)$, P *(2)

What is your interpretation of the Marginal revenue function $\mathrm{R} *(\mathrm{x})$ in this problem?
f) What is your interpretation of your Marginal cost function in this problem, vis-à-vis fixed cost?

## [20 marks]

## SECTION C (COMPULSORY)

[40 MARKS]

You borrow \$ 30000 from the bank for purposes of paying for your Post-graduate Project. If Interest is charged at the rate of $16 \%$ Compounded quarterly and the loan is for a period of 2 years,
a) Calculate the Regular payment, R.
b) Construct the relevant Amortization schedule.
c) How much is outstanding after the $6^{\text {th }}$ payment?
d) What are the Interest and Capital portions of the $5^{\text {th }}$ payment?

## QUESTION EIGHT

a) What are the problems(points to note) in the construction of Index numbers?
[8 marks]
b) The table below shows the unit price and quantity of rice, sugar and salt consumed by a certain household in 1996 and 1998.

|  | 1996 |  | 1998 |  |
| :--- | :--- | :--- | :--- | :--- |
| PRODUCT | PRICE \$ | QUANTITY(KG) | PRICE \$ | QUANTITY(KG) |
| RICE | 12 | 25 | 18 | 15 |
| SUGAR | 24 | 30 | 37 | 24 |
| SALT | 2,7 | 6 | 6,5 | 6 |

(1996=100)
Calculate:
i) The Unweighted Aggregative Price Index.
ii) Fischer's Ideal Index
[12 marks]
[Total: 20 marks]

