## QUANTITATIVE ANALYSIS FOR BUSINESS CIN 1207 SUPPLEMENTARY EXAM

JULY 2005
DURATION: 3 HOURS
INSTRUCTIONS TO CANDIDATES

1. Answer all questions in Section A
2. Choose and answer five(5) out of six(6) questions in Section B
3. Graph paper will be provided on request
4. Statistical tables will be provided
5. You may use a non-programmable Scientific Calculator

## SECTION A (ANSWER ALL QUESTIONS) [40 MARKS]

## QUESTION ONE

a) The rate of inflation in Zimbania over the last five years was $13 \% ; 18 \% ; 20 \%$; $30 \% ; 40 \%$. Find the average rate of inflation in Zimbania over the five year period.
[3marks]
b) A company proposes to sell 50 Kg of Copper at $\$ 40$ per Kg and 60 Kg Silicon at $\$ 50$ per Kg . Calculate the price per Kg for a combined package.
[4 marks]
c) In the state lotteries, how many 6-digit numbers can be formed from the 10 digits $0-9$, if repetitions are allowed?
[2 marks]
d) List:
i) Three (3) methods of data collection.
[3 marks]
ii) Three (3) methods of sampling.
[3 marks]
e) A fair die is rolled once. What is the probability that it turns in a value which is at most 4 ?
[2 marks]
f) A pair of fair dice is rolled once. What is the probability that the sum on the dice is:
i) an even number?
[3marks]
ii) at least 3 ?
[4 marks]
g) A motorist travels at $150 \mathrm{~km} / \mathrm{h}$ over a 50 km stretch of road, and $130 \mathrm{~km} / \mathrm{h}$ over another hilly 50 km portion. Find the motorist's overall average speed over the entire journey?
[4 marks]
h) How many different sums of money can be obtained by choosing two coins from a box containing a 5 cent coin, a 10 cent coin, a 20 cent coin, a 50 cent coin and a $\$ 1$ coin?
[2 marks]
i) How many arrangements can we make from the letters of the word
"Mississippi?"
[2 marks]
j) Define the terms:
i) Conditional probability.
ii) Dependent events.
iii) Inclusive events.
iv) Discrete data.
[8 marks]
Total [40 marks]

## SECTION B: CHOOSE AND ANSWER 5 OUT OF 6 QUESTIONS

## ALL QUESTIONS CARRY EQUAL MARKS

## QUESTION TWO

A real estate company specializing in sales of farms would like to know if their sales can be predicted based on the number of years of experience of their salespersons. A random sample of sales is taken for 10 salespeople having years of experience ranging from 1 to 10 years and is given below:

| Years of experience | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of sales | 3 | 2 | 5 | 4 | 6 | 8 | 9 | 9 | 12 | 10 |

i) Plot the scatter graph for the data.
[4 marks]
ii) Find the sample regression equation using the Least Squares method.
[6 marks]
iii) Predict sales for someone with 15 years experience, from the Least Squares equation.
[3 marks ]
iv) Compute the co-efficient of determination and comment. [7 marks ]

Total [20 marks]

## QUESTION THREE

| Firm | DEFECTIVE TUBES PER BOX OF 100 UNITS |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{0}$ | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ or more | Total |
| Supplier A | 500 | 200 | 200 | 100 | $\mathbf{1 0 0 0}$ |
| Supplier B | 320 | 160 | 80 | 40 | $\mathbf{6 0 0}$ |
| Supplier C | 600 | 100 | 50 | 50 | $\mathbf{8 0 0}$ |
| Total | $\mathbf{1 4 2 0}$ | $\mathbf{4 6 0}$ | $\mathbf{3 3 0}$ | $\mathbf{1 9 0}$ | $\mathbf{2 4 0 0}$ |

i) If one box had been selected at random from this universe, what are the probabilities that the box would have come from supplier A? Supplier B?
[2 marks, 2marks]
ii) If a box was selected at random, what is the probability that it would contain two defective tubes?
[4 marks]
iii) If a box came from supplier A, what is the probability that the box would have 2 or less defectives?
iv) It is known that a box selected at random has two defective tubes, what is the probability that it came from supplier A? from suppler B? from supplier C?
[4 marks, 4marks,4marks] Total [20 marks]

## QUESTION FOUR

The following figures relate to credit reports prepared by a credit reporting agency for 100 business days:

| 60 | 43 | 64 | 58 | 52 | 52 | 67 | 59 | 60 | 51 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 62 | 56 | 63 | 61 | 68 | 57 | 51 | 59 | 47 | 42 |
| 64 | 43 | 67 | 52 | 58 | 47 | 59 | 64 | 58 | 52 |
| 63 | 48 | 65 | 60 | 61 | 59 | 63 | 56 | 62 | 56 |
| 62 | 57 | 59 | 62 | 56 | 63 | 55 | 73 | 60 | 69 |
| 53 | 66 | 54 | 52 | 54 | 61 | 55 | 65 | 55 | 61 |
| 59 | 74 | 62 | 49 | 63 | 63 | 53 | 71 | 59 | 46 |
| 64 | 41 | 60 | 51 | 55 | 64 | 46 | 64 | 56 | 59 |
| 49 | 64 | 60 | 57 | 58 | 66 | 53 | 65 | 62 | 58 |
| 65 | 61 | 50 | 55 | 57 | 61 | 45 | 43 | 60 | 66 |

i) Construct a frequency distribution table starting at 40, using an interval width of 5 .
[6 marks]
ii) From the grouped frequency distribution in i) above, calculate the
a) mean.
b) median.
c) mode

## QUESTION FIVE

The local chamber of commerce has commissioned some market research into the spending habits of the local adult population. A random sample of 500 adults has been selected as follows:
Age group (years) Number in sample

$$
18-<21 \quad 54
$$

$21-<30 \quad 63$
$30-<45 \quad 167$
$45-<60 \quad 85$
60 and over 131

From Government census statistics, it is known that the local adult population has the following distribution:

| Age group (years) | \% of population |
| :--- | :--- |
| $18-<21$ | 13 |
| $21-<30$ | 12 |
| $30-<45$ | 38 |
| $45-<60$ | 15 |
| 60 and over | 22 |

What comment can you make about the age profile of the selected sample compared to that of the population (Carry out a Chi-squared test using $\alpha=5 \%$ ). Total [20 marks]

## QUESTION SIX

a) A foreman is concerned about the amount of time that workers spend in the rest- room. A random sample of 12 workers in one day gave the following times in minutes: $\quad 3 ; 5 ; 4 ; 3 ; 2 ; 4 ; 4 ; 1 ; 3 ; 3 ; 5 ; 5$; Give the $95 \%$ prediction interval.
b) 400 zippers are inspected and 74 are found to be defective. Give the $99 \%$ confidence interval estimate of the population proportion of defective zippers.
[5 marks]
c) A sample of 150 light bulbs of type A gave a mean life of 1400 hours and a standard deviation of 120 hours. Another sample of 200 light bulbs of type B gave a mean life of 1200 hours and a standard deviation of 80 hours.
Determine a $95 \%$ confidence interval for the difference between the mean life spans of the two types of light bulbs.
[10 marks]
Total [20 marks]

## QUESTION SEVEN

a) In a survey of pig farms it is suspected that the occurrence of a particular disease may be associated with the method of feeding. Methods of feeding are grouped into two categories, A and B. Of 27 farms on which the disease occurred, 16 used method A and of 173 farms on which the disease had not occurred, 84 used method A. Test using the $5 \%$ level of significance, for independence between the method of feeding and occurrence of disease.
[10 marks]
A sample length of material was cut from each of five randomly selected rolls of cloth and each length divided into two halves. One half was dyed with a newly developed dye and the other half with a dye that had been in use for some time. The ten pieces were then washed and the amount of dye washed out was recorded for each piece as follows:-

| Roll | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |
| Old dye | 13.2 | 13.7 | 15.4 | 13.5 | 16.8 |
| New dye | 12.5 | 14.3 | 16.8 | 14.9 | 17.7 |

Investigate the allegation that the amount of dye washed out for the old dye is significantly less than for the new dye (use $\alpha=0.05$ )

[10 marks]<br>Total [20 marks]

***END OF EXAMINATION***

