## NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY

## B. COMM (HONOURS) DEGREE IN ACTUARIAL SCIENCE

## FINANCIAL ECONOMICS : CIN 4115

## JULY 2004 SUPPLIMENTARY EXAMINATION

## DURATION : 2 HOURS

## INSTRUCTIONS TO CANDIDATES

1. Attempt all questions
2. You must not start writing your answers in the booklet until instructed to do so by the invigilator.
3. In addition to this question paper, you require an electronic calculator (non-programmable)
4. An investor can choose between 2 investments A and B.

Investment A - the rate of return is distributed uniformly between 4\% and 10\% Investment B - The rate of return can take only discrete values with the following probabilities

| Probability | B |
| :---: | :--- |
| $1 / 5$ | $12 \%$ |
| $1 / 5$ | $10 \%$ |
| $1 / 5$ | $8 \%$ |
| $2 / 5$ | $3 \%$ |

For each investment calculate
(a) Mean
[2 marks]
(b) Variance
(c) Semi-variance
(d) The shortfall probability with level of 6\% [6 marks]
(e) The mean shortfall with level of 5\%
2. An investor makes his investment decisions based on the log utility function
$\bigcup(w)=$ luw, $\quad w>0$ where $w$ denotes his wealth at the end of the period of investment
(a) Show that this investor is non-satiated and risk-averse. [6 marks]
(b) The investor above has initial wealth of $\$ 20000$. He could invest all his wealth in cash for one year at a guaranteed rate of return of $5 \%$ per annum. Alternatively he could invest entirely in shares which over the year have equal probability of earning a rate of return of $10 \%$ per annum or of $2 \%$ per annum.

Determine whether the investor should choose cash or shares.
[8 marks]
3. An investor is faced with three independent investment portfolios $\mathrm{A}, \mathrm{B}$ and C .

Each has the following rate of returns:
A: $3 \%, 5 \%$ and $7 \%$ with probabilities $\frac{1}{4}, \frac{1}{2}, \frac{1}{2}$ respectively
B: $4 \%, 5 \%$ and $6 \%$ with probabilities $1 / 3,1 / 3,1 / 3$ respectively
C: $3 \%, 5 \%$ and $7 \%$ with probabilities $1 / 5,{ }^{2} / 5,2 / 5$ respectively
Using each of the following types of dominance which portfolio would an investor choose first, second and third?
(a) Absolute dominance
[2 marks]
(b) First order stochastic dominance
[3 marks]
(c) Second order stochastic dominance
4. Assume the CAPM holds
(a) (i) What constitutes the market portfolio in the CAPM?
[4 marks]
(ii) Give the definitions for the Capital Market line and the Security Market Line. Define all terms you use.
[7 marks]
(iii) Give an interpretation for the terms in the equation of the Capital Market Line.
[4 marks]
(b) Assume the beta of a security is either
(i) $\beta=0$ or
(ii) $\beta<0$

Compare the expected return of this security in both cases with the $\cap 3 k-$ free rate of return and given an explanation of your observations.
[8 marks]
[Total 23 marks]
5. Explain the three forms of efficient market hypothesis (EMH) [9 marks]
6. An investor chooses to invest in equities from two counters Boc and Naschco. Boc equities have an expected return of $5 \%$, with standard deviation $15 \%$. Naschco equities are more risky, their expected returned is $10 \%$ with standard deviation $25 \%$. The correlation coefficient of the two equity markets is 0.3 .
(i) Given that the investor has $\alpha$ invested in Boc shares and $1-\alpha$ invested in Naschco shares, state equations for the expected return and standard deviation for the investor's portfolio.
[8 marks]
(ii) The investor is allowed to invest both long and short in Boc and Maschco equities. Prove that the investor's opportunity set in $\bar{R}-\sigma$ space is a hyperbola with equation $\sigma^{2}=a \bar{R}^{2}+b \bar{R}+\mathrm{c}$

Find the values for $\mathrm{a}, \mathrm{b}$ and c .
[6 marks]
[Total 14 marks]
7. A risky security, A has expected return $13 \%$ and variance of return $100 \% \%$. You are advised that the risk-free rate of return is $\$ \%$.
(i) Given that A is an efficient portfolio, derive the equation for the capital market line.
[6 marks]
(ii) The expected return on the market (M) is 9\%. Using your result in part (i) above calculate the variance of the return on the market. [5 marks]
[Total 11 marks]
END OF EXAMINATION PAPER

