## NATI ONAL UNI VERSI TY OF SCI ENCE AND TECHNOLOGY FACULTY OF I NDUSTRI AL TECHNOLOGY <br> DEPARTMENT OF I NDUSTRI AL AND MANUFACTURI NG ENGI NEERI NG <br> Bachelor of Engineering Honours Degree I ndustrial \& Manufacturing Engineering

## Fluid Mechanics - TI E 2202 <br> $2^{\text {nd }}$ SEMESTER EXAMI NATI ONS AUGUST, 2009

## INSTRUCTIONS TO CANDIDATES

## Time : 3 hours

Answer 5 questions
QUESTION . 1
a) Derive the equation of continuity for fluid flow.
b) Define the following terms used in connection with the flow of a
Liquid
i) uniform flow [2]
ii) steady flow[2]

iii) unsteady flow ..... [2]
iv) discharge ..... [2]
v) mass flow rate ..... [10]

## QUESTION 2

Derive Bernoulli's equation for the flow of an incompressible frictionless fluid from the consideration of momentum.

## QUESTION 3

Water flows through a pipe AB diameter whose diameter is 1.2 m at $3 \mathrm{~m} / \mathrm{s}$ and then passes through a pipe BC, 1.5 m in diameter. At C the pipe fork, branch CD is 0.8 m in diameter and carries one third of the flow in AB . The velocity in branch CE is $2.5 \mathrm{~m} / \mathrm{s}$

## Find:

a) the volume rate of flow in AB
b) the velocity in BC
c) the velocity in CD
d) the diameter of CE

## QUESTION 4

a) Summarise the objectives of the eight chapters that have been covered in Fluid Mechanics.
b) Discuss the implication of the momentum equation as far as fluid flow is concerned.

## QUESTION 5

a) A pipe line carries water at the rate of $1.5 \mathrm{~m}^{3} / \mathrm{s}$ from 1 reservoir to another which is 3 km away and 45 m lower. The diameter of the pipe is 40 mm . Assume that the friction factor for a smooth pipe is given by

$$
f=\frac{\tau w}{\frac{1}{2} \rho u^{2}}=0.046 \mathrm{Re}^{-0.2}
$$

Where $\tau \mathrm{w}$ is the wall shear stress, $\rho$ is density, u is the mean velocity in the pipe and Re is the Reynolds number, and for water the density is $1000 \mathrm{~kg} / \mathrm{m}^{3}$ and the dynamic viscosity is $1.0 \times 10^{-3} \mathrm{Ns} / \mathrm{m}^{2}$. What will be the power required to maintain flow?
b) Show that from Euler's equation for the energy transfer between impeller and fluid the head is given by:

$$
\begin{equation*}
\mathrm{E}=(\mathrm{U} / \mathrm{g})\left(\mathrm{u}-\mathrm{V}_{\mathrm{f}} \operatorname{Cos} \beta^{1}{ }_{2}\right) \tag{10}
\end{equation*}
$$

## QUESTION 6

Show that in a fully developed laminar flow of a fluid through a pipe of radius $r$ and length $L$, the velocity profile and the flow rate are given by:
(a)

$$
\mu=-\frac{R^{2}}{4 \mu}\left(\frac{\partial p}{\partial x}\right)\left[1-\left(\frac{r}{R}\right)^{2}\right]
$$

(b)

$$
Q=\frac{\prod \Delta p D^{4}}{128 \mu \mathrm{~L}}
$$

## QUESTION 7

A $45^{\circ}$ reducing pipe bend in a horizontal plane tapers from 600 mm diameter at inlet to 300 mm diameter at outlet. The gauge pressure at inlet is 140 kPa and the rate of flow of water through the bend is $0.425 \mathrm{~m}^{3} / \mathrm{s}$. Neglecting friction, calculate the net resultant force exerted by the water on the bend.

## QUESTION 8

(a) Define the following terms in relation to boundary layer theory.
(i) Boundary layer thickness $\sigma$
(ii) Displacement thickness $\sigma^{*}$
(iii) Momentum thickness
(b) In a two dimension, laminar boundary layer flow along a flat plate, boundary layer velocity profile is
$\frac{u}{U}=\sin \left(\frac{\Pi}{2} \frac{y}{\sigma}\right)$ for $0 \leq y \leq \sigma$
and $\frac{u}{U}=1$ for $y=\sigma$

Find:
(i) $\quad \delta(\mathrm{x})$ disturbance thickness
(ii) $\quad \delta^{*}(\mathrm{x})$ displacement thickness
(iii) Total frictional force on a plate of length L , and width, b .

## END OF EXAM

