# NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY <br> FACULTY OF THE BUILT ENVIRONMENT <br> BACHELOR OF QUANTITY SURVEYING (HONOURS) DEGREE <br> PART II SUPPLEMENTARY EXAMINATIONS - JULY 2014 <br> STATISTICS II - AQS 2209 

Time: 3 hours
Total Marks: 100
INSTRUCTIONS TO CANDIDATES
Answer ONLY FOUR questions
Each question carries ( 25 marks).

A1. The results of a survey at a big Construction and Quantity Surveying Consultancy firm made to determine whether the age of a driver 21 years of age and older has any effect on the number of automobile accidents in which he or she is involved are shown in the table below.

|  | Age of Driver |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :---: |
| Number of <br> Accidents | $21-30$ | $31-40$ | $41-50$ | $51-60$ | $61-70$ |  |
| 0 | 748 | 821 | 786 | 720 | 672 |  |
| 1 | 74 | 60 | 51 | 66 | 50 |  |
| 2 | 31 | 25 | 22 | 16 | 15 |  |
| Greater than 2 | 9 | 10 | 6 | 5 | 7 |  |

(a) Test at $5 \%$ level of significance that the number of accidents is independent of the age of the driver.
(b) Test at $10 \%$ level of significance that the number of accidents is independent of the age of the driver.
(c) What possible sources of difficulty in sampling techniques, as well as other considerations, could affect your conclusions?

A2. The table below shows the heights to the nearest millimetre and weights to the nearest pound (lb) of a sample of 12 pavers drawn at random from a brick manufacturing company.

| Height, X <br> $(\mathrm{mm})$ | 70 | 63 | 72 | 60 | 66 | 70 | 74 | 65 | 62 | 67 | 65 | 68 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Weight, Y <br> (lb) | 155 | 150 | 180 | 135 | 156 | 168 | 178 | 160 | 132 | 145 | 139 | 152 |

(a) Draw a scatter diagram of $y$ against $x$ on graph paper. Fit the least squares straight line to these data and draw your fitted line on your scatter diagram.
[10 marks]
(b) Carry out an analysis of variance (ANOVA) to test at the $5 \%$ level of significance whether the slope is significantly different from zero. From your ANOVA table, compute the coefficient of determination, $\mathrm{r}^{2}$, and interpret it. [9 marks]
(c) Predict the weight of the paver if the height is 63.
[3 marks]
(d) Predict the height when the weight is known to be 168 lb .
[3 marks]

A3. (a) Define the following terms as they are used in experimental design:
I. Randomisation
II. Blocking
III. Treatment
(b) A product development engineer is interested in investigating the tensile strength of a new reinforcement that will be used to make lintels. The engineer knows from past experience that the strength of the lintels is affected by the weight of reinforcement used. The engineer decides to test 5 levels of reinforcement strengths (treatments) which are 15, 20, 25, 3 and 35 and decides to use 5 replicates as shown in the table below:

| REINFORCEMENT <br> STRENGTH | 1 |  |  |  |  |  |  | OBSERVATIONS <br> 3 |  |  |  |  | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 7 | 7 | 15 | 11 | 9 |  |  |  |  |  |  |  |  |  |
| 20 | 12 | 17 | 12 | 18 | 18 |  |  |  |  |  |  |  |  |  |
| 25 | 14 | 18 | 18 | 19 | 19 |  |  |  |  |  |  |  |  |  |
| 30 | 19 | 25 | 22 | 19 | 23 |  |  |  |  |  |  |  |  |  |
| 35 | 7 | 10 | 11 | 15 | 11 |  |  |  |  |  |  |  |  |  |

A4. (a) Explain the advantages of using Latin Squares in Experimental Design.
[5 marks]
(b) Consider the table below of a Latin Square design for analysing rocked propellant where both batches of raw materials and operators represent randomisation.

| BATCHES OF <br> RAW MATERIALS | 1 |  |  |  |  |  | 2 |  |  |  | OPERATORS <br> 3 |  | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\mathrm{~A}=-1$ | $\mathrm{~B}=-5$ | $\mathrm{C}=-6$ | $\mathrm{D}=-1$ | $\mathrm{E}=-1$ |  |  |  |  |  |  |  |  |  |
| 2 | $\mathrm{~B}=-8$ | $\mathrm{C}=-1$ | $\mathrm{D}=5$ | $\mathrm{E}=2$ | $\mathrm{~A}=11$ |  |  |  |  |  |  |  |  |  |
| 3 | $\mathrm{C}=-7$ | $\mathrm{D}=13$ | $\mathrm{E}=1$ | $\mathrm{~A}=2$ | $\mathrm{~B}=-4$ |  |  |  |  |  |  |  |  |  |
| 4 | $\mathrm{D}=1$ | $\mathrm{E}=6$ | $\mathrm{~A}=1$ | $\mathrm{~B}=-2$ | $\mathrm{C}=-3$ |  |  |  |  |  |  |  |  |  |
| 5 | $\mathrm{E}=-3$ | $\mathrm{~A}=5$ | $\mathrm{~B}=-5$ | $\mathrm{C}=4$ | $\mathrm{D}=6$ |  |  |  |  |  |  |  |  |  |

(b) Test at 0.05 level of significance if there is difference between batches and raw materials.
[20 marks]

A5. (a) Discuss the advantages and applications of factorial designs. [5 marks]
(b) A manufacturer wishes to determine the effectiveness of four types of machines ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D ) in the production of bolts used in construction. To accomplish this, the numbers of defective bolts produced by each machine in the days of a given week are obtained for each of two shifts; the results are shown in the table below:

|  |  | Replicates |  |  |  |  |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- |
| Factor 1: <br> Machine | Factor 11: <br> Shift | Mon | Tue | Wed | Thur | Fri |
| A | 1 | 6 | 4 | 5 | 5 | 4 |
|  | 2 | 5 | 7 | 4 | 6 | 8 |
| B | 1 | 10 | 8 | 7 | 7 | 9 |
|  | 2 | 7 | 9 | 12 | 8 | 8 |
| C | 1 | 7 | 5 | 6 | 5 | 9 |
|  | 2 | 9 | 7 | 5 | 4 | 6 |
| D | 1 | 8 | 4 | 6 | 5 | 5 |
|  | 2 | 5 | 7 | 9 | 7 | 10 |

Perform an analysis of variance to determine at 0.05 level of significance whether there is a difference:
(a) Between the machines
(b) Between the shifts
[20 marks]

A6. A construction firm wishes to investigate the effects of advertising on the sales. The advertising and sales data for the past three years 2011 to 2013 are shown in the table below:

| Advertising <br> expenditure, <br> X, (US\$) | 1000 | 1200 | 1800 | 1500 | 800 | 1700 | 2000 | 1500 | 1100 | 1900 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sales, Y, <br> (US\$) | 22000 | 25000 | 26000 | 30000 | 23000 | 27000 | 32000 | 27000 | 25000 | 29000 |

(a) Draw a scatter diagram of $y$ against $x$ on graph paper.
(b) Find the least squares straight line to these data and draw your fitted line on your scatter diagram.
(b) Compute the correlation coefficient and interpret it.
(c) Predict the sales when the advertising cost is $\$ 1950$

