# NATIONAL UNIVERSITY OF SCIENCE AND TECHNOLOGY 

 FACULTY OF COMMERCEDEPARTMENT OF FINANCE
BACHELOR OF COMMERCE HONOURS DEGREE IN FINANCE
Optional for: Accounting, Banking, Insurance \& Risk Management, Marketing, and Management
PART I 1 ${ }^{\text {ST }}$ SEMESTER FINAL EXAMINATION - DECEMBER 2006
FINANCIAL MATHEMATICS I [CFI 1101]
TIME ALLOWED: 3 HOURS 10 MINUTES

## INSTRUCTIONS

1. The paper is 3 hours and 10 minutes.
2. Answer any $\boldsymbol{F O U R}$ questions.
3. Start each question on a fresh page.
4. All workings must be shown.

## Question 1

[25 marks]
1.1 The yield on 91 day commercial paper is $24 \%$, and the discount rate on similar risk Bankers` Acceptance with same maturity is $22 \%$. Which security are you going to purchase? Explain. [5 marks]
1.2 An investor purchases a 91 day TB 20 days after issue at a rate of discount of $30 \%$ and sells it 30 days before maturity at a rate of discount of $32 \%$.

### 1.2.1 Calculate the realized yield. <br> [15 marks]

1.2.2 Distinguish between realized yield and promised yield. [5 marks]

Question 2 [25 marks]
2.1 You are faced with two investment options whose interest is determined as as follows:

- $\quad 44 \%$ per annum compounded semi annually.
- $43 \%$ per annum compounded monthly.

Which investment should you choose? Explain
[10 marks]
2.2 You invest $\$ 20000$ today the rate of interest of $36.5 \%$ compounded daily in order harvest $\$ 30000$ at some future date? What is your investment horizon?
[15 marks]

## Question 3 <br> [25 marks]

3.1 Show that the present value of a growing ordinary annuity is

$$
\frac{(1+i)^{n}-(1+g)^{n}}{(i-g)(1+i)^{n}}
$$

$$
\begin{array}{rll}
\text { Where } n & = & \text { number of periods } \\
i & = & \text { compound interest per period } \\
g & = & \text { annuity growth rate }
\end{array}
$$

3.2 A Charity Fund is set up to pay $\$ 10000$ at the beginning of each quarter for 5 years. How much should be invested today if interest of $24 \%$ is capitalized monthly?
[13 marks]
Question 4 [25 marks]

The terms of a mortgage loan are:

- Price $\$ 24000000$
- $25 \%$ Deposit
- Interest $48 \%$ compounded monthly for 25 years.
- Principal and interest to be amortized by equal monthly payments.
4.1 Calculate the monthly payment
[8 marks]
4.2 Calculate the Buyer's and Seller's equity at the end of 10 years [10 marks]
4.3 Calculate the monthly payment if at the end of 10 years the Building Society adjusts interest to $45 \%$, compounded monthly, and if the term of the loan remains the same.
[7 marks]


## Question 5

[25 marks]
5.1 A loan of $\$ 10000000$, bearing $40 \%$ simple interest, to be paid half yearly, must be discharged at the end of 4 years by means of a sinking fund which earns $24 \%$ interest compounded quarterly.
5.1.1 Calculate the quarterly deposit into the Fund [10 marks]
5.1.2 Calculate the annual cost of servicing the debt.
[5 marks]
5.2 Discuss, in brief, the attributes of a capital budgeting appraisal method whose objective is owner value maximization.
[10 marks]

