

#### FACULTY OF COMMERCE DEPARTMENT OF FINANCE BACHELOR OF COMMERCE HONOURS DEGREE IN FINANCE PART I 2ND SEMESTER SUPPLEMENTARY EXAMINATION - AUGUST 2011 <u>FINANCIAL MATHEMATICS II [CFI 1201]</u> TIME ALLOWED: 3HOURS

# **INSTRUCTIONS TO CANDIDATES**

- 1. Attempt any FOUR questions
- 2. Start the answer to each full question on a fresh page of the answer sheet.
- 3. Questions may be written in any order, but must be legibly numbered.
- 4. Write legibly, showing all workings.

# **INFORMATION TO CANDIDATES**

- 1. Each Question carries a total of 25 marks.
- 2. The businesses in this question paper are intended to be fictitious
- 3. The paper contains FOUR (4) QUESTIONS.

# **Question One**

- (a) An investor purchases a \$1000, 10% coupon bond at a price yielding 11% p.a over 20 years. Coupons are payable annually.
   Calculate:
  - (i) The equilibrium price of the bond. [5 marks]
  - (ii) The investor's realized yield if yields increase to 12% at the end of 10 years and the investor holds the bond to maturity. [5 marks]
  - (iii) The investor's holding period yield if yields increase to 12% at the end of 10 years and the investor sells the bond at the end of 17 years. [5 marks]
- (b) Given results in (ii) and (iii) of (a) above, determine, giving reasons, whether the bond duration is below or above 17 years. [6 marks]
- (c) Discuss any <u>**TWO**</u> weaknesses of duration analysis as an approach to bond risk analysis.

[4 marks]

Total [25 marks]

# **Question Two**

An analyst has estimated the following return distributions for stocks A and B:

State of the	Probability	Return on A (%)	Return on B (%)
economy			
Boom	0.3	20	7
Normal	0.6	15	16
Slump	0.1	5	22

Using the information in the table above, determine:

(i)	The expected return and standard deviation of A and B.	[4;6 marks]
(ii)	The covariance of returns for A and B.	[3 marks]
(iii)	The correlation coefficient of returns of A and B.	[2 marks]

	(iv)	The expected return and standard deviation of a portfolio invested 40% in A and				
		60% in B.	[2;3 marks]			
	(v)	The minimum variance portfolio comprising stocks A and B.	[5 marks]			
		Total	[25 marks]			
Question Three						
(a)	Define	the following risks associated with bonds:				
	(i)	Interest rate risk	[4 marks]			
	(ii)	Reinvestment rate risk	[3 marks]			
(b)	(b) Consider a \$1000, 10% coupon bond that is issued at a price of \$962 and has a term to					
	maturity of 5 years, with coupons payable annually.					
	Calculate:					
	(i)	The yield to maturity of the bond	[4 marks]			
	(ii)	The Macaulay duration of the bond	[6 marks]			
	(iii)	The Convexity of the bond	[5 marks]			
	(iv)	The approximate change in the value of the bond following a decrease in yields to				
		10.5%	[3 marks]			
		Total	[25 marks]			

# **Question Four**

- (a) Shawntel Ltd is a public company that has just paid a dividend of \$2.00 per share. The company's shares are currently trading at \$46 and dividends are expected to grow at a constant rate of 5.4% indefinitely. The return on equity (ROE) for the company is 15%. Calculate:
  - (i) The implied required return on equity (k<sub>e</sub>) for Shawntel Ltd. [3 marks]
  - (ii) The implied payout ratio [3 marks]
  - (iii) The value per share if investors believe that the dividend growth rate will be 7%
     p.a for the first four years and 5.4% thereafter. (NB: Assume the same k<sub>e</sub> as in (i) above) [5 marks]
- (b) Distinguish between net operating cash flow and free cash flow to equity. [2 marks]

(c) The yield on 4-year treasury bonds is 15% and that on 3-year Treasury notes is 12%. Determine the implied 1-year forward rate 3 years from now. [3 marks]
(d) Briefly explain the following term structure theories:

(i)	The Liquidity Preference Theory	[3 marks]
(ii)	The Segmentation Theory	[3 marks]
(iii)	The Rational Expectations Theory	[3 marks]

#### Total [25 marks]

#### **Question Five**

- (e) State any <u>FOUR</u> assumptions underlying Modern Portfolio Theory (MPT). [4 marks]
- (f) Determine whether each of the following portfolios is efficient given the following equation for the Capital Market Line (CML):  $R_p = 0.06 + 0.6\sigma_p$  [8 marks]

Portfolio	Expected Return	Standard Deviation
	(%)	(%)
А	8	5
В	9.9	6.5
С	9	5
D	11	8

- (g) Interest rates are 8% and 5% in South Africa and in the US respectively. According to the International Fischer Effect (IFE), what is the expected depreciation in the South African rand? [3 marks]
- (h) Show that the condition:  $\frac{i_{h-i_f}}{1+i_f} = \frac{r_{h-r_f}}{1+r_f}$  is consistent with the IFE; where  $i_h$  and  $i_f$  are home and foreign inflation rates respectively and  $r_h$  and  $r_f$  are home and foreign nominal interest rates respectively. [6 marks]

Total [20 marks]

# END OF EXAMINATION PAPER