

FACULTY OF APPLIED SCIENCE

DEPARTMENT OF STATISTICS AND OPERATIONS RESEARCH

SBA 4102 ALGORITHMS AND HEURISTICS

DECEMBER 2024 EXAMINATION

Time : 3 hours

Candidates should attempt **ALL** questions from Section A and **ANY THREE** questions from Section B. Each question should start on a fresh page.

SECTION A

Answer **ALL** questions in this section [40 Marks]

- A1.** State any two factors that can be used to evaluate the performance of an algorithm. [2]
- A2.** Explain any five characteristics of an algorithm. [10]
- A3.** (a) Explain the difference between divide and conquer and dynamic programming. [4]
(b) Explain the Traveling Salesman Problem (TSP) and why it is considered an NP-hard problem. [5]
- A4.** (a) Write down mathematical formal definition of big O notation. [3]
(b) Suppose two algorithms perform the same task, explain how you will determine the more efficient one. [6]
- A5.** Illustrate asymptotic and complexity analysis of algorithms. [10]

SECTION B

Answer any **THREE** questions in this section [60 Marks]

- B6.** (a) Distinguish between $O(n!)$ - factorial time and $O(1)$ - constant time big O notations. [4]
- (b) Explain the insertion sort algorithm's time complexity. [4]
- (c) Compare and contrast insertion sort and merge sort in terms of time complexity and use case. [4]
- (d) Write down algorithm to sort the following list of integers (6, 20,15,1,4) using the Insertion Sort algorithm. [12]
- B7.** (a) What is a flow chart? [1]
- (b) Distinguish between algorithms and heuristics. [4]
- (c) Why is the big O notation important in analyzing algorithms? [3]
- (d) What is Dijkstra's algorithm and what type of problems does it solve? [4]
- (e) Explain the Traveling Salesman Problem and why it is considered an NP-hard problem. [8]
- B8.** (a) What are greedy algorithms. [2]
- (b) Explain how the Kruskal's algorithm works to come up with a minimum spanning tree [11]
- (c) Interpret the following output produced after executing Kruskal's algorithm to link the four cities. [5]

Following are the edges in the constructed MST
2 -- 3 == 4
0 -- 3 == 5
0 -- 1 == 10

Graph for Kruskal's Algorithm with MST Highlighted

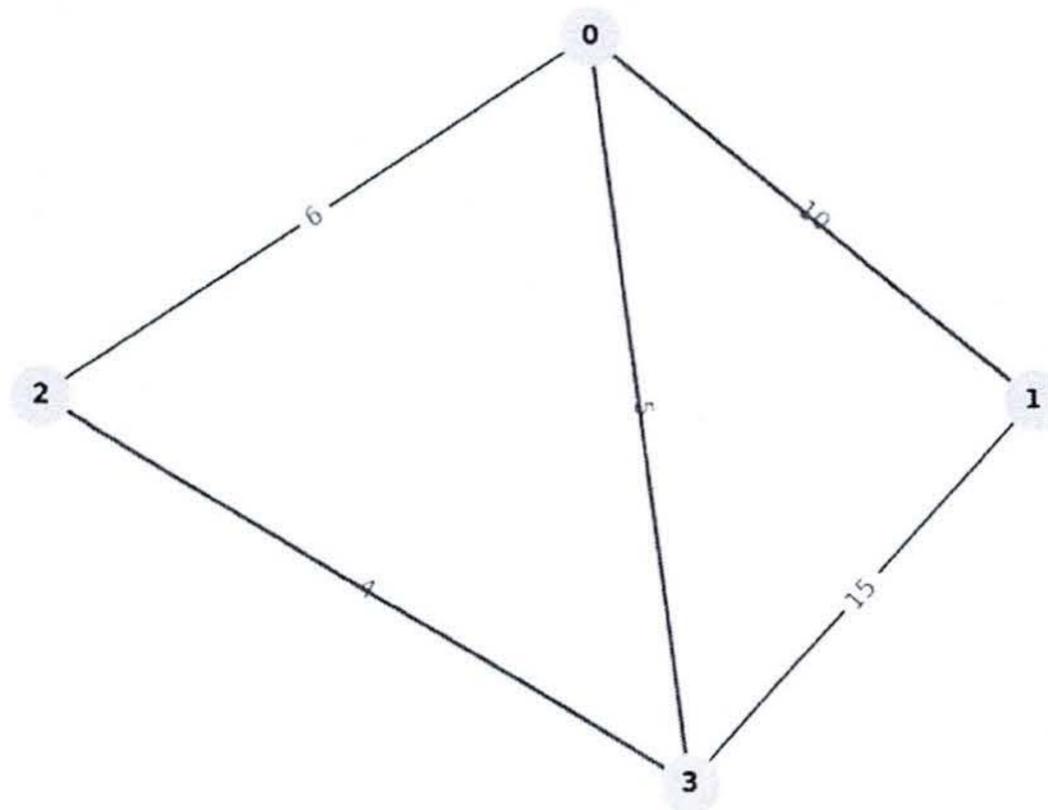


Figure 1: Minimum Spanning Tree Output

(d) What is the optimal distance to connect all the cities basing on the above output. [2]

B9. (a) What are machine learning algorithms? [2]

(b) Explain the steps presented by the following machine learning algorithm. [10]

```

1 import numpy as np
2 from sklearn.linear_model import LinearRegression
3 import matplotlib.pyplot as plt
4
5 # Sample data
6 X = np.array([[1], [2], [3], [4], [5]])
7 y = np.array([1, 3, 2, 3, 5])
8
9 # Create and train the model
10 model = LinearRegression()
11 model.fit(X, y)
12
13 # Make predictions
14 predictions = model.predict(X)
15
16 # Plot the results
17 plt.scatter(X, y, color='blue')
18 plt.plot(X, predictions, color='red')
19 plt.xlabel('X')
20 plt.ylabel('y')
21 plt.title('Linear Regression')
22 plt.show()

```

Figure 2: Machine Learning Algorithm Python Code

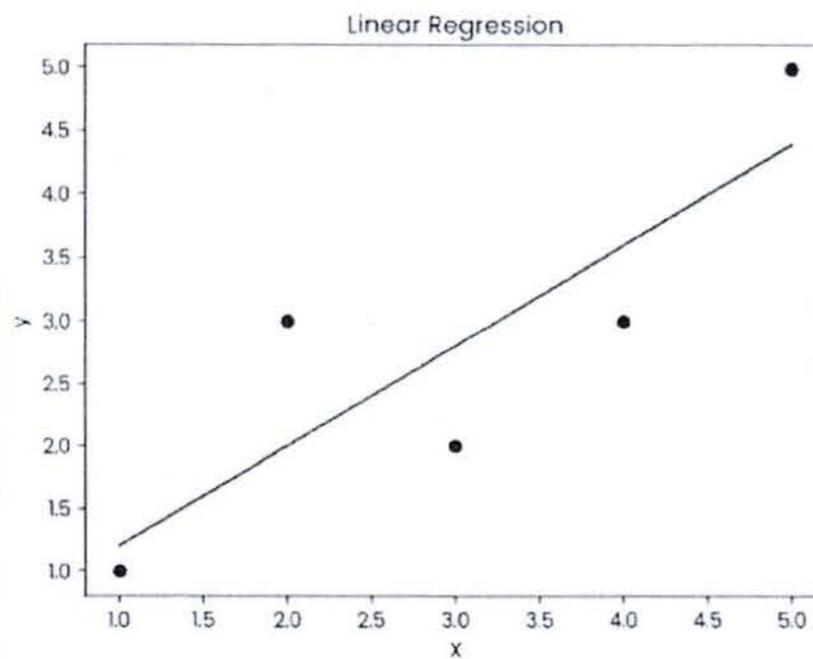


Figure 3: Machine Learning Algorithm Python Code Corresponding Output

- (c) Explain the model's time complexity and where it can be implemented. [5]
- (d) Interpret the output produced. [3]

END OF QUESTION PAPER